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Roll No. ....

Total Questions : 13 ]

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B.C.A. IVth Semester Examination, May-2019

**MATHEMATICS-III**

(BCA-306)

Time : 3 Hrs. ]

[ M.M. : 75

Note :- Attempt all the Sections as per instructions.

**Section-A**

(Very Short Answer Type Questions)

Note :- Attempt all the five questions. Each question carries 3 marks.

1. Find the order and degree of the differential equation :

$$\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^4 + y = 0$$

2. State Leibnitz test.

Or

Cauchy's root test.

3. Express  $1 - i$  in the modulus amplitude form.

4. If  $r = \sin t \hat{i} + \cos t \hat{j} + \hat{k}$ , find :

(i)  $\frac{dr}{dt}$

(ii)  $\left| \frac{dr}{dt} \right|$

5. Solve :

$$\frac{d^2y}{dx^2} - 7\frac{dy}{dx} + 12y = 0$$

**Section-B**

(Short Answer Type Questions)

Note :- Attempt any two questions out of the following three questions. Each question carries 7½ marks.

6. If  $z_1$  and  $z_2$  are any complex numbers, then prove that :

$$|z_1 + z_2|^2 + |z_1 - z_2|^2 = 2(|z_1|^2 + |z_2|^2)$$

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7. Solve :

$$(1 + x^2)dy = (1 + y^2)dx$$

8. Prove that :

$$\lim_{n \rightarrow \infty} \frac{1}{n} (1 + 2^{1/2} + 3^{1/3} + \dots + n^{1/n}) = 1$$

### Section-C

#### (Long Answer Type Questions)

Note :- Attempt any *three* questions out of the following five questions. Each question carries 15 marks.

9. (a) If  $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \pi$ , then prove that :

$$x + y + z = xyz$$

(b) Test the convergence of the series whose  $n$ th term is :

$$\sqrt{n+1} - \sqrt{n}$$

10. Find the directional derivative of  $f(x, y, z) = x^2yz + 4xz^2$  at the point  $(1, -2, -1)$  in the direction of the vector  $2\hat{i} - \hat{j} - 2\hat{k}$ .

11. Find the Fourier series for the function  $f(x) = |x|$ ,  $-\pi < x < \pi$ . Hence deduce that :

$$\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$$

12. (a) Solve :

$$\frac{d^2y}{dx^2} + 9y = \cos 2x + \sin 2x$$

(b) Solve :

$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{-3x}$$

13. (a) Solve :

$$(e^y + 1) \cos x \, dx + e^y \sin x \, dy = 0$$

(b) Solve :

$$(x + 2y^3) \frac{dy}{dx} = y$$